

$X \sim \text{Unif}(0,1)$ $Y \sim \text{Unif}(0,1)$ X and Y are independent.

$\Rightarrow f(x,y) =$ _____

$\Rightarrow F_X(a) = F_Y(a) =$ _____

Let $A = \max(X, Y)$. What is the pdf of A ?

$F_A(a) =$ _____

def. of the cdf

$=$ _____

def of A

$= P(X \leq a \cap Y \leq a)$

$=$ _____

independence

$=$ _____

$=$ _____

□

$f_A(a) =$ _____

$=$ _____

□

Extra "credit" generalise to:

* X and Y with any known cdf

* $X_1, X_2, X_3, \dots, X_n$ indep with known cdf

$$A = \max(X_1, X_2, \dots, X_n)$$