

MLE

Invariance: $\widehat{f(\theta)} = f(\hat{\theta})$

Eg. if $\hat{\lambda} = \bar{x}$

$\Rightarrow \hat{\lambda}^2 = \bar{x}^2$

$(\hat{1/\lambda}) = 1/\bar{x}$

NOT TRUE
FOR OTHER
ESTIMATORS!

$$\text{Var}(\hat{\lambda}_{ML}) = \text{Var}(\bar{x}_n)$$

$$= \frac{1}{n^2} \sum \text{Var}(x_i) = \frac{\text{Var}(x_i)}{n}$$

How might we estimate that?

$$\widehat{\text{Var}}(\hat{\lambda}_{ML}) = \frac{\widehat{\text{Var}}(x)}{n} = \frac{\sum (x_i - \bar{x})^2}{n^2}$$

↑
estimated
variance of
estimator